



## **Closer Look at the Contracting Solar Nebula**

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### **Authors' contributions**

*This work was carried out in collaboration between both authors. Both authors read and approved the final manuscript.*

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### **ABSTRACT**

Rawal [1 to 11] studied the contraction of the Solar Nebula in order to understand the formation of the Solar System and to derive Planetary Distance Law. He took the view that the Solar Nebula contracted in steps of Roche Limit. Roche Limit is defined as the three dimensional distance on entering which the secondary body breaks into pieces due to tidal forces of the primary. Alternatively, it is the three-dimensional distance within which the primordial matter which is left behind around the primary, after its formation, does not get condensed into a secondary, due to tidal forces of the primary. In his paper entitled "Contraction of the Solar Nebula", Rawal (aforementioned papers) took the assumption that the ratio of the density of the primary ( $\rho_p$ ) to the density of the secondary ( $\rho_s$ ), which appears in the formula of Roche Limit, is of the order unity, that is,  $(\rho_p/\rho_s) = 1$ . In order to get closer look in the contraction of the Solar nebula, here, in this paper, we would like to remove this restriction on the ratio  $(\rho_p/\rho_s)$  and take it to be 0.7, 0.8, 0.9 or 1.1, 1.2, 1.3

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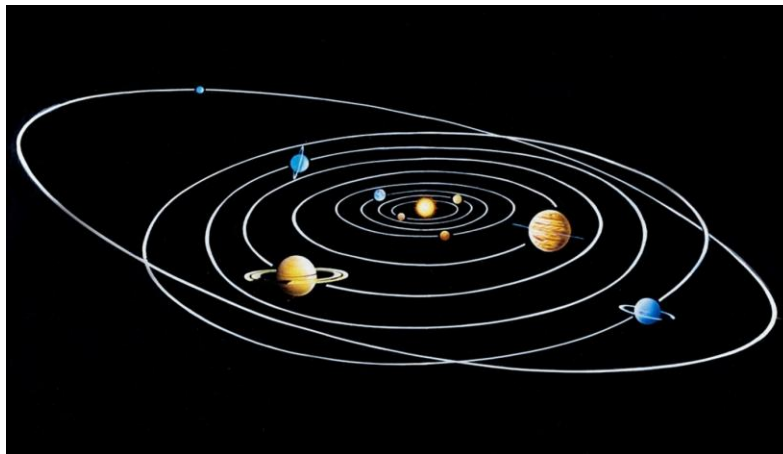
and derive the distances of outer and inner edges of the gaseous rings, which one by one, go to form secondaries around the primary (here, the Sun), out of which planets were formed. This may give us closer look of the contraction of the Solar Nebula which is going to form the Solar System, giving rise to the form of Planetary Distance Law, consistent with 2/3-stable Laplacian Resonance Relation, which may be closer to reality. After going through this exercise, it is found, here, that the assumption that  $(\rho_p/\rho_s)=1$  may be relaxed. If it is less than 1, the system is shrunk and if it is more than 1 the system expands, only the Scale-parameter changes, the structure remains similar. However, in all these cases resonance necessarily will not be stable 2/3-Laplacian resonance. For stable 2/3-Laplacian resonant orbits, the ratio  $(\rho_p/\rho_s) = 1$  is utmost necessary. One, therefore, concludes that the orbits in the Solar System are stable because the ratio  $(\rho_p/\rho_s)$  involved in the Roche Limit, is of the order unity.

*Keywords: Contracting solar nebula; closer look.*

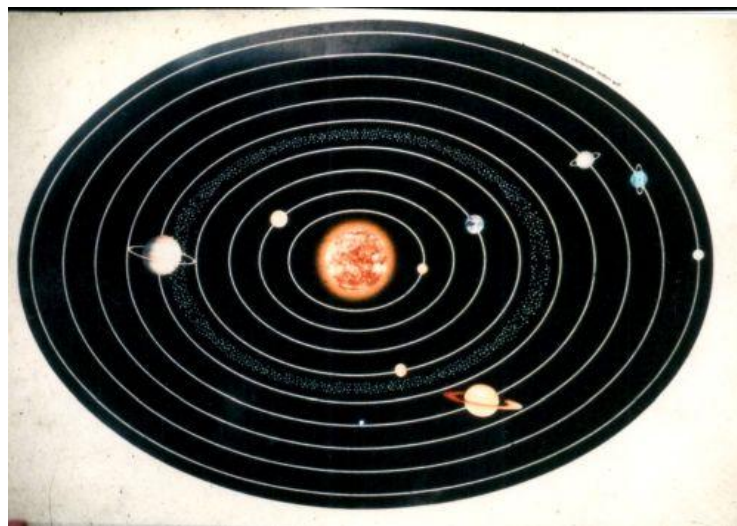
## 1. INTRODUCTION

Since the time Copernicus (1542) pronounced that the planets revolve around the Sun,

astronomers have been trying to understand the formation of the Solar System (Figs. 1, 2). Numerous theories for the formation of the Solar System have, so far, been advanced [1,3].



**Fig. 1. The solar system**



**Fig. 2. The solar system**

Among all these theories of the formation of the Solar System, Laplace's nebular hypothesis is favoured, as it explains (1) the isotopic abundance of the elements in the Solar System and in the Universe, (2) the estimates of the ages of the Sun and the planets, (3) Our understanding of transformation of a hot magnetic and rotating interstellar gas cloud into a star, (4) chemical and mineralogical composition of different objects in the Solar System such as meteorites, (5) Coplanarity of the orbital radii of almost all planets in the Solar System, (6) rotational directions of all planets, except Venus, are the same as the direction of rotation of the Sun, (7) directions of revolutions of all planets are the same as rotational direction of the Sun indicating the co-genetic origin and (8) support from astronomical observations [12]. However, it faced the following problems: (1) the problem of explaining extraordinary character of the distribution of mass and angular momentum in the Solar System, (2) the problem of explaining why the protosun shaded a discrete system of gaseous rings in which planets were formed and (3) the problem of explaining how the planets were aggregated from each gaseous ring [1 to 11].

The difficulties faced by Laplacian hypothesis were considered [13,14,15] and [13,14,15]. They presented an outline of the Laplacian theory, which they call modern Laplacian theory for the formation of the Solar System. They considered the influence of a supersonic turbulent convection and the radial turbulent stress in the cloud and showed that how this radial turbulent stress led to the formation and detachment of a discrete system of gaseous rings when the inward gravitational force balanced the outward centrifugal force, the ratio of the orbital radii  $R_p/R_{p-1}$  of successively disposed gaseous rings being a constant, forming a geometrical progression (Fig. 3), [12,13,14,15,16,17,18] and [1 to 11].

However, the ratio of the orbital radii  $R_p$  of successively disposed gaseous rings that they obtained is, of course, a constant forming a geometrical progression, but it does not lead to correct distances of planets after two or three steps, as the geometrical progression proceeds outward. Also, it is not found consistent with Kepler's third law of Planetary motion, and also with Laplace's stable 2/3 – resonance relation. It cannot generate Planetary Distance Law and even cannot explain the existence of rings around the central body.

## 1.1 Roche Limit

Roche Limit (Fig. 4) is defined as the three dimensional distance around the Primary on entering which the secondary body breaks into pieces due to tidal forces of the primary. Alternatively, it is the three-dimensional distance within which the primordial matter which is left behind around the primary, after its formation, does not get condensed into a secondary, due to tidal forces of the primary. Roche Limit [4] is given by

$$d_{\text{Roche}} = 1.442 \left[ \rho_p / \rho_s \right]^{1/3} \times R \quad (1.1)$$

where,  $R$  is the radius of the primary (the central body, here, the Sun),  $\rho_p$  is the density of primary and  $\rho_s$  is the density of secondary.

Rawal (1984) assumed  $(\rho_p / \rho_s) = 1$  so that

$$d_{\text{Roche}} = 1.442 R \quad (1.2)$$

If we denote the Roche constant 1.44 which appears in Roche Limit formula as 'a' for convenience, we write

$$d_{\text{Roche}} = a R \quad (1.3)$$

Trying to understand the formation of the Solar System, [4] took the view that the solar nebula had contracted by steps of Roche Limit to form the Solar System. In this process, it was also seen that the phenomenon of supersonic turbulent convection and the radial turbulent stress described in [13,14,15,16] were operative and when the inward gravitational force became equal to the outward centrifugal force, a ring of material was shaded out (disposed of) (Fig. 6). This brought about a momentary halt at various stages of contraction. His aim was an attempt to understand and explain, on the basis of concept of Roche Limit and the Laplacian stable 2/3-resonance Relation the discrete distribution of planets, that is, planetary distance law in the Solar System and try to understand the physics underlying the formation of planetary System and the physical meaning of constants involved in the Planetary Distance Law.

In his paper, entitled "Contraction of the Solar Nebula", [14] took the assumption that the ratio of the density of the primary ( $\rho_p$ ) to the density of the secondary ( $\rho_s$ ) which appears in the formula of Roche Limit is of the order unity, that is,  $(\rho_p / \rho_s) = 1$ , and derived the Planetary Distance

Law in the form  $r_n = R_0 a^n$ ,  $n=1, 2, 3, \dots, k$ , where  $R_0$  is the radius of the primary, here, the Sun, and 'a' is a pure constant, we call it as the Roche Constant, the value of which, in the Solar System, is 1.442 (See Table 1).

In order to get closer look at the contracting Solar Nebula, here, in this paper, we would like

to remove the restriction on the ratio  $(\rho_p/\rho_s)$  which appears in the formula of Roche Limit to be of order unity and take it to be 0.7, 0.8, 0.9 or 1.1, 1.2, 1.3 and derive the distances of outer and inner edges of the gaseous rings which, one by one, go to form secondaries, around the primary (here, the Sun), out of which planets were formed.

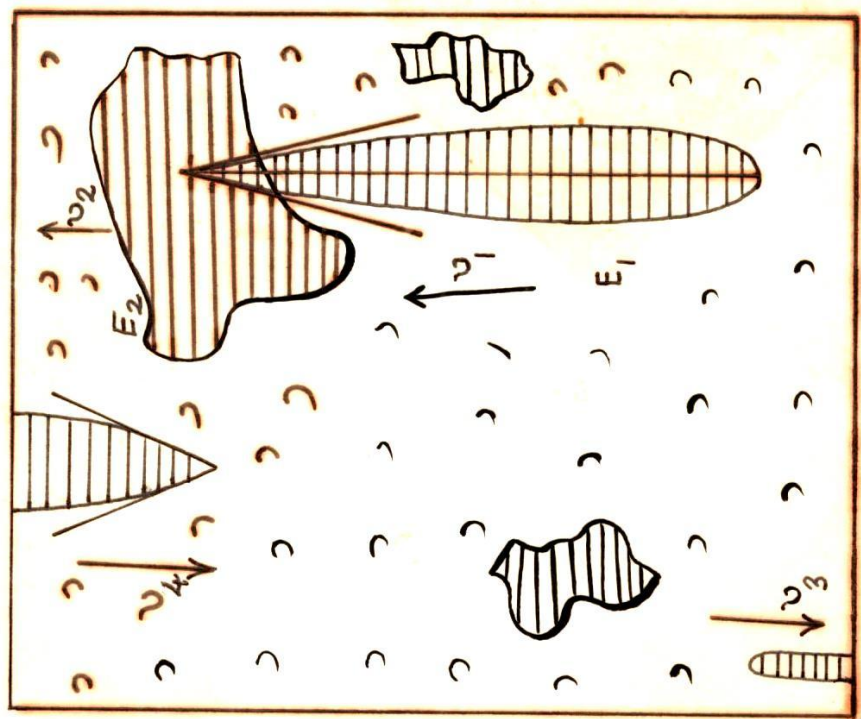


Fig. 3. Supersonic turbulent convection

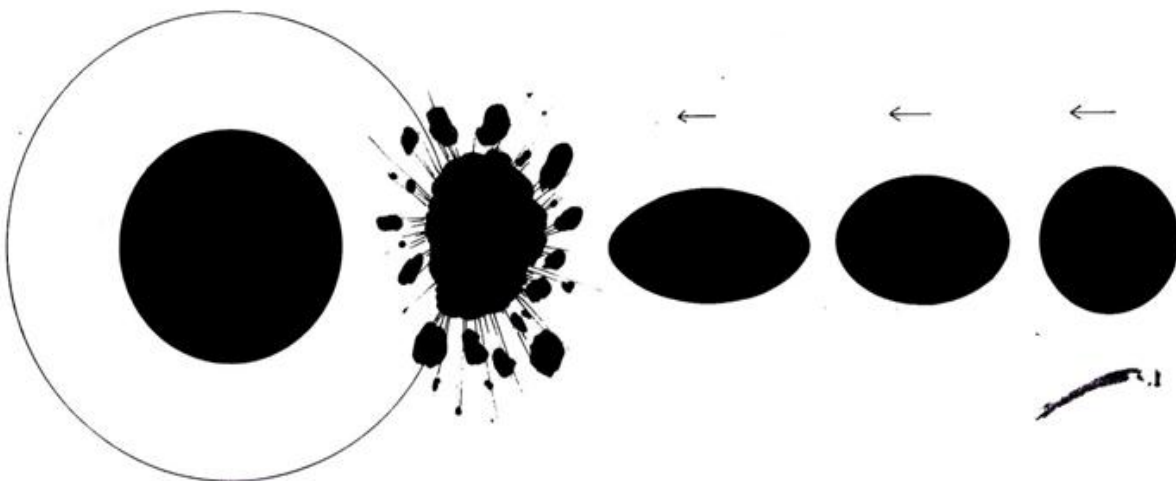


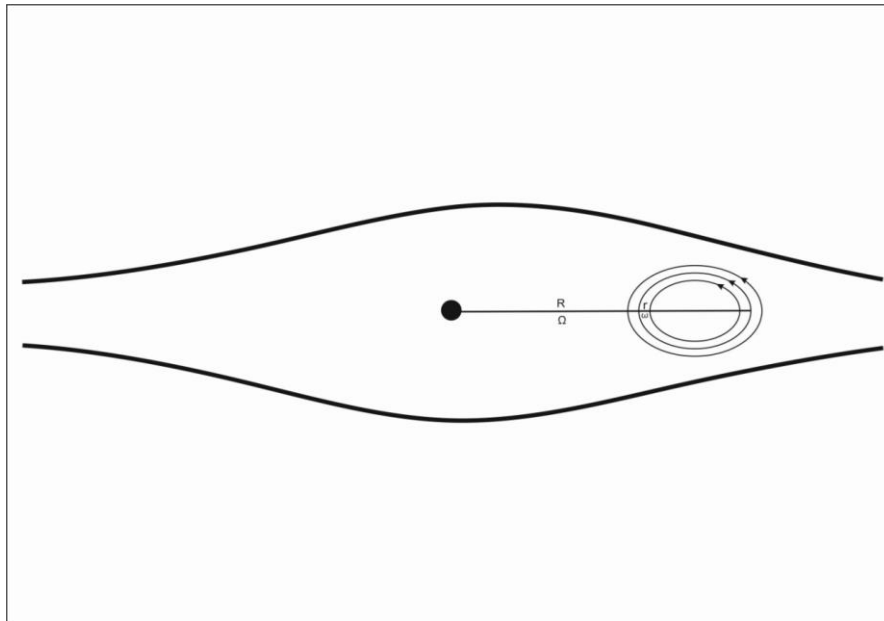
Fig. 4. Roche limit

## 2. CONTRACTING SOLAR NEBULA

It is assumed that there was a spinning spherical gas cloud of interstellar gas and dust with mass,  $M$ , slightly greater than  $M_{\odot}$  ( $M_{\odot}$  = Sun's Mass), and certain radius, denoted by  $R_p$ . Under the influence of its self-gravitation, the cloud began to contract and due to the principle of conservation of angular momentum, it began to spin faster and faster as the nebula went on to contracting. Solar nebula also went onto bulging at the equator as it went to rotate faster and faster. A stage was reached at which the outward centrifugal force became equal to the inward gravitational force at the equator, at which point the gravitational and rotational instability arose along with supersonic turbulent convection and the radial turbulent stress, consistent with stable 2/3-Laplacian resonance relation. Laplacian Resonance Relation is [10]:  $n_1 - 3n_2 + 2n_3 = 0$  where  $n_1, n_2, n_3$  are mean motions of triads of successive planets around the Sun. This resulted into a shell of gaseous matter which evolved into a ring of gaseous matter at the equator and got detached. This whole process got repeated itself, till the solar nebula reached its present size, in which form, we call it, the Sun. Here, the contraction of the above solar nebula halting at various radii is described in a particular fashion given below (Fig. 6). In this process, it is seen that the halts at various radii are being brought

about by the phenomena of supersonic turbulent convection and the radial turbulent stress, when the outward centrifugal force became equal to the inward gravitational force, consistent with stable 2/3-Laplacian resonance relation. The supersonic turbulent convection does the following jobs: (1) It creates an additional source of outward pressure in a solar nebula called the radial turbulent stress which helps halt momentarily the free collapse of the Solar nebula by releasing a ring of matter, first at the dimensions of the Limit of the planetary system [6], (2) it causes the interior of the solar nebula to rotate almost uniformly like a rigid body due to a large turbulent viscosity and also drastically lowers the moment-of-inertia coefficient 'f' of the protosun, thereby, allowing the protosun to give up its angular momentum to a very light planetary system and (3) it leads to the formation of a very dense ring of gas and dust at the equator of the protosun, thereby, causing the protosun to dispose of its excess angular momentum through the successive detachment of a discrete system of rings of gas and dust.

Consider that the Solar nebula has initial radius  $R_p$  (Figs. 6 and 7). Assume that the Solar nebula has shrunk to a radius  $R_{p-1}$  for which  $R_p$  is the Roche Limit of the cloud with radius  $R_{p-1}$  (Figs. 6, 7, 8).



**Fig. 5. Depending upon the mass of the nebula and its distance from the galactic centre, The Milky Way Galaxy assigns the Limit to the solar nebula out of which the Solar System was formed Gravitational collapse in the nebula starts from the limit of its span. This is the boundary to the Solar System**

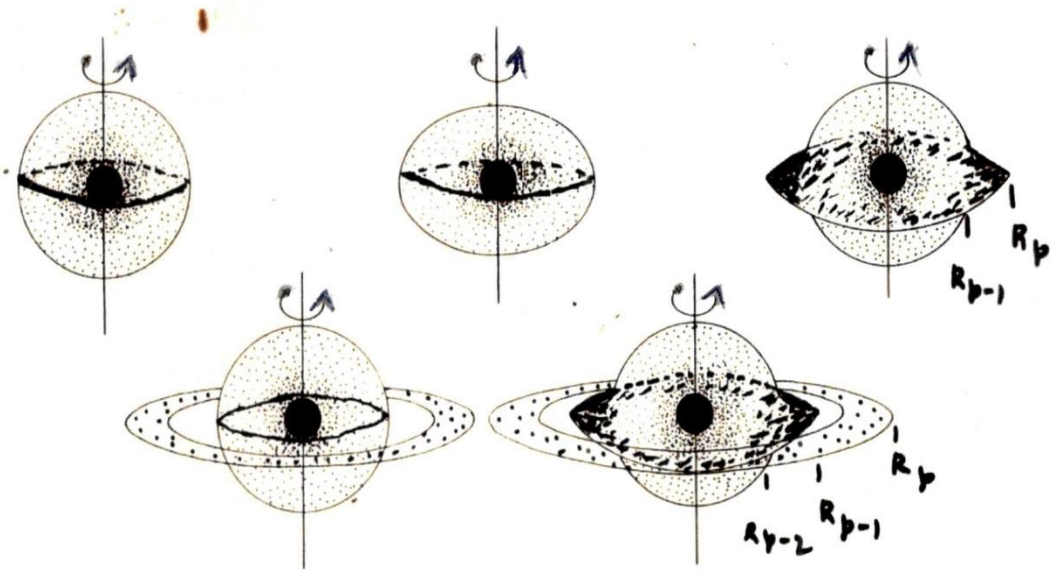
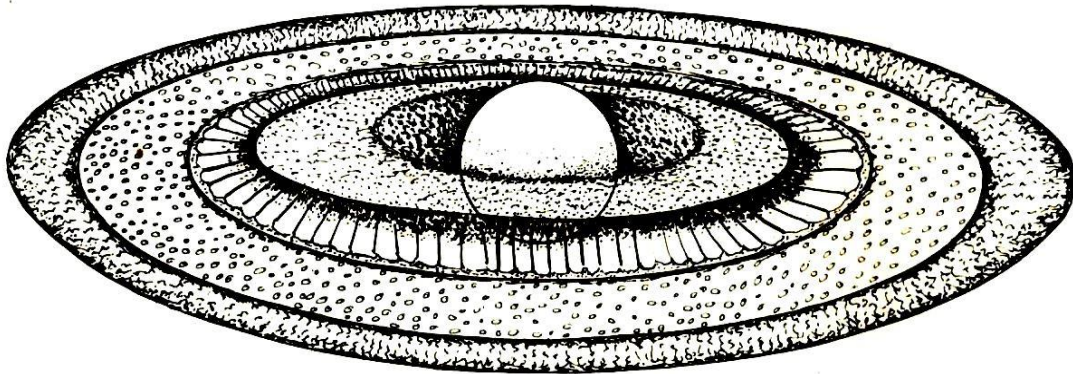


Fig. 6.



Schematic diagram showing the formation of the Solar System and the Satellite Systems of planets on the basis of contraction of the solar and sub-solar nebulae in terms of Roche Limit in the background of Modern Laplacian Theory.

Fig. 7.



**Fig. 8.**

Therefore, relation between  $R_p$  and  $R_{p-1}$  of the contracting spherical gas cloud (Solar nebula) can be written as

$$R_p = a R_{p-1} \quad (2.1)$$

The three-dimensional shell of gas and dust (matter) having width  $R_p - R_{p-1}$  forms the Roche zone of the protosun having radius  $R_{p-1}$ . The matter in the shell having width  $R_p - R_{p-1}$  forms a bulge at the equator of the rotating gas cloud and settles down to form a ring of matter at the equator of width  $R_p - R_{p-1}$ . The matter inside such a ring grows to form planetesimals, but cannot form a full secondary (planet) there, because the matter inside such a ring is still inside the Roche Limit of the protosun having radius  $R_{p-1}$ . The matter inside such a ring has to wait for further contraction of the solar nebula to take place, so that it comes out of Roche Limit of the spherical cloud of gas and dust to form a full secondary (planet) there.

At the next stage of contraction of the Solar nebula, the cloud shrinks to a radius  $R_{p-2}$  such that

$$R_{p-1} = a R_{p-2} \quad (2.2)$$

Therefore, eqn. (2.1) takes the form

$$R_p = a. (a R_{p-2}) = a^2 R_{p-2} \quad (2.3)$$

The annular ring ( $R_{p-2}, R_{p-1}$ ) of width ( $R_{p-1} - R_{p-2}$ ) lies inside the Roche Limit of the protosun then having radius  $R_{p-2}$ . At this stage, the previous ring ( $R_{p-1}, R_p$ ) of matter comes out of the Roche zone of the protosun having radius  $R_{p-2}$ , and the matter inside it, grows to form a planet, as it has come out of the Roche Limit.

Rawal (1984) assumed that the contraction of the Solar nebula proceeded in this fashion till the solar nebula reached its present size, in which form, we call it, the Sun, the halts at various radii were being brought about by the phenomena of supersonic turbulent convection and the radial turbulent stress, at the point at which the outward centrifugal force at the equator became equal to inward gravitational force, consistent with stable Laplacian 2/3-resonance relation, eventually leading us to the stage.

$$R_1 = a R_\odot \quad (2.4)$$

Where  $R_\odot$  is the radius of the present Sun. In terms of the radius of the present sun, the sequence of the radii of the contracting Solar nebula at various stages of the contraction can be expressed as

$$R_p = R_{\odot} a^p, \quad p = 1, 2, 3, 4, \dots, k \quad (2.5)$$

Table 1, shows various  $R_p$ . The known planet residing in the ring labelled  $(R_{p-1}, R_p)$  for various values of  $p$  are also mentioned.

On this scheme, eqn. (2.5) is looked upon as giving rise to outer and inner boundaries of

various rings. The scenario, here, brings out that the ring structure feature is common and natural feature of the heavenly bodies, in particular, of the major members of the Solar System such as Jupiter, Saturn, Uranus, Neptune, our sun and even our own Milky Way Galaxy (Figs. 8, 9, 10, 11, 12, 13, 14, 15). It is obvious that the distant planets were formed earlier.

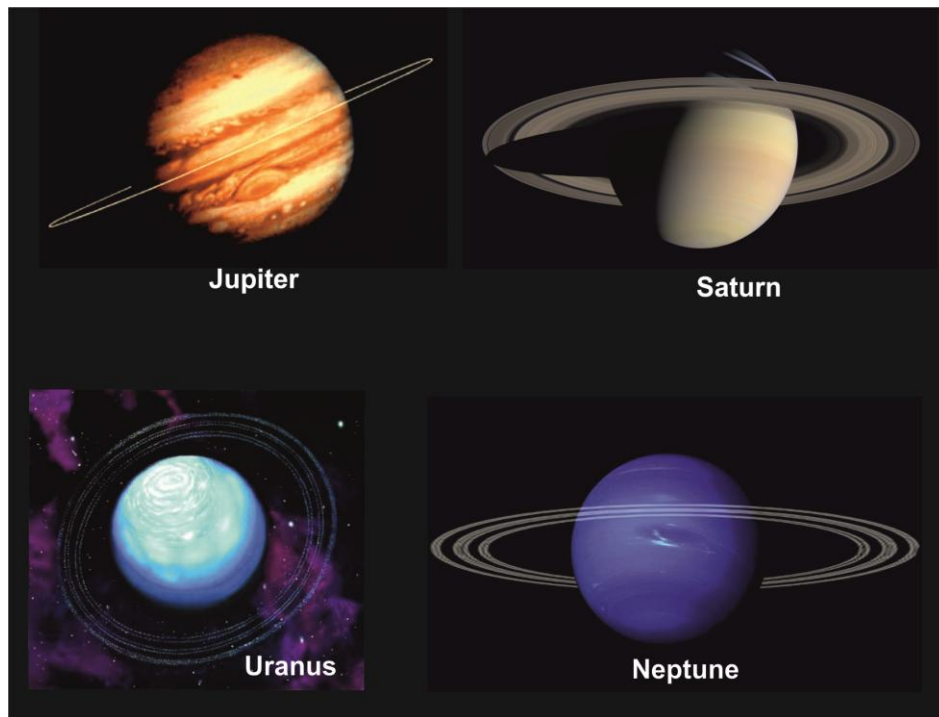


Fig. 9. Rings around the Planets

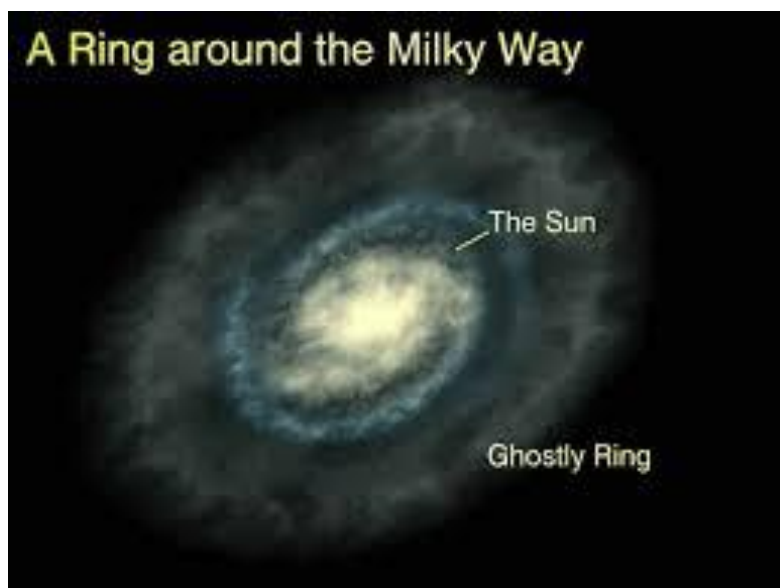


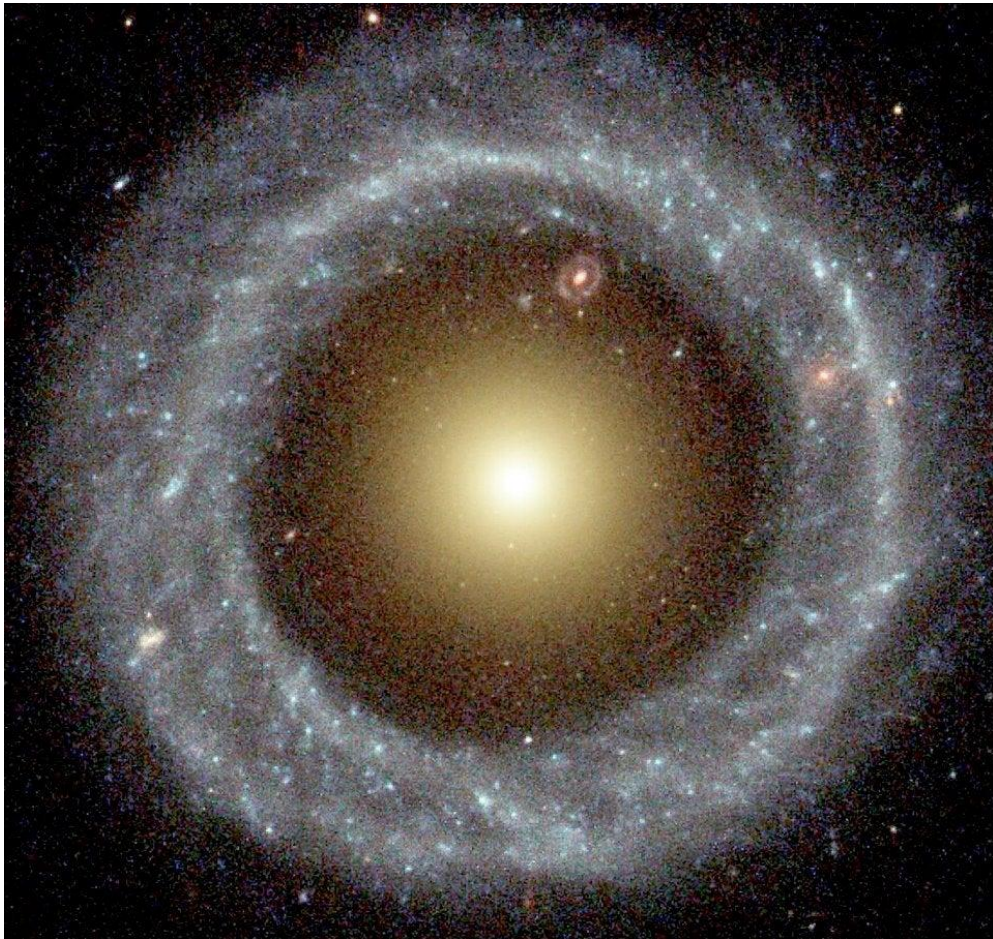
Fig. 10.



**Fig. 11. Rings around the galaxy**



**Fig. 12. Rings around the Galaxy**



**Fig. 13. Rings around the Galaxy**



**Fig. 14. Rings around the Galaxy**

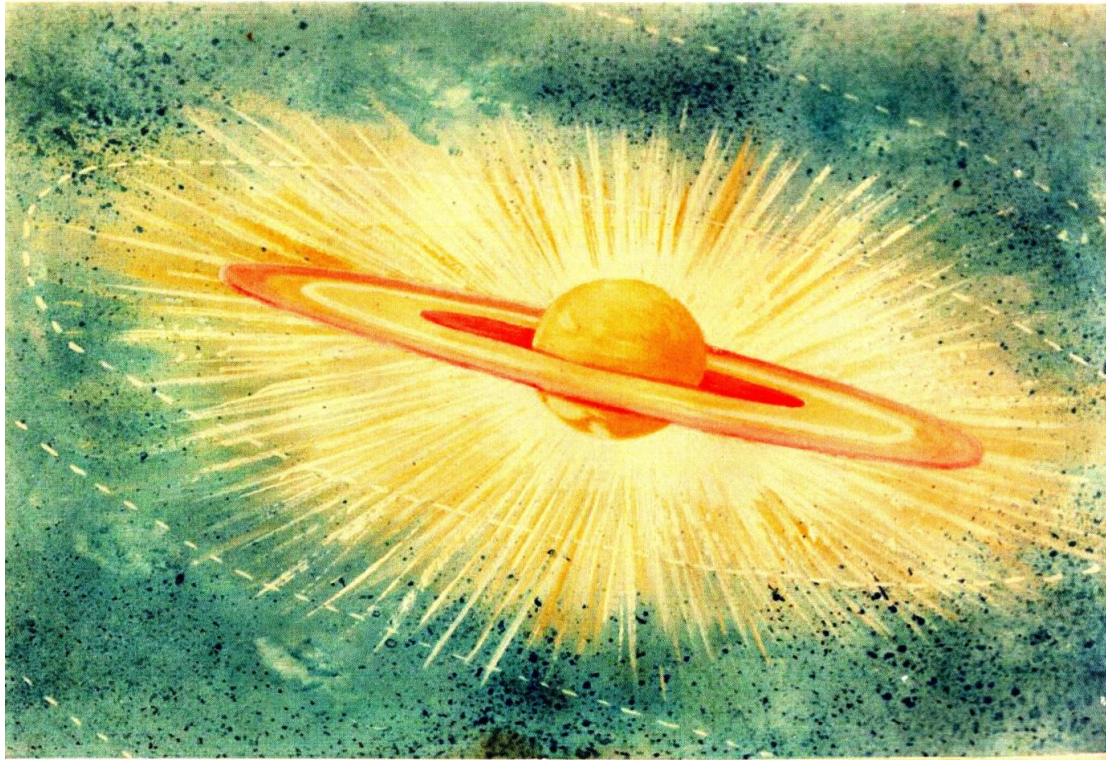


Fig. 15. Rings around the Sun

Table 1.

| $R_p$ , the radius of the contracting Solar nebula in units of AU | Annular ring ( $R_{p-1}, R_p$ ) | Width $R_p - R_{p-1}$ of the annular ring ( $R_{p-1}, R_p$ ) in units of AU | Mean radius of the annular ring ( $R_{p-1}, R_p$ ) in units of AU | Known Object in the annular ring ( $R_{p-1}, R_p$ ) | Observed mean distance of the known object in the annular ring ( $R_{p-1}, R_p$ ) in units of AU |
|-------------------------------------------------------------------|---------------------------------|-----------------------------------------------------------------------------|-------------------------------------------------------------------|-----------------------------------------------------|--------------------------------------------------------------------------------------------------|
| $R_0 = 0.004652$                                                  |                                 |                                                                             |                                                                   |                                                     |                                                                                                  |
| $R_1 = 0.007$                                                     | $(R_0, R_1)$                    | 0.0024                                                                      | 0.006                                                             | –                                                   | –                                                                                                |
| $R_2 = 0.01$                                                      | $(R_1, R_2)$                    | 0.003                                                                       | 0.008                                                             | –                                                   | –                                                                                                |
| $R_3 = 0.014$                                                     | $(R_2, R_3)$                    | 0.004                                                                       | 0.012                                                             | –                                                   | –                                                                                                |
| $R_4 = 0.02$                                                      | $(R_3, R_4)$                    | 0.006                                                                       | 0.017                                                             | –                                                   | –                                                                                                |
| $R_5 = 0.03$                                                      | $(R_4, R_5)$                    | 0.01                                                                        | 0.025                                                             | –                                                   | –                                                                                                |
| $R_6 = 0.042$                                                     | $(R_5, R_6)$                    | 0.012                                                                       | 0.036                                                             | –                                                   | –                                                                                                |
| $R_7 = 0.06$                                                      | $(R_6, R_7)$                    | 0.018                                                                       | 0.051                                                             | –                                                   | –                                                                                                |
| $R_8 = 0.087$                                                     | $(R_7, R_8)$                    | 0.027                                                                       | 0.073                                                             | –                                                   | –                                                                                                |
| $R_9 = 0.13$                                                      | $(R_8, R_9)$                    | 0.043                                                                       | 0.11                                                              | –                                                   | –                                                                                                |
| $R_{10} = 0.18$                                                   | $(R_9, R_{10})$                 | 0.05                                                                        | 0.155                                                             | –                                                   | –                                                                                                |
| $R_{11} = 0.26$                                                   | $(R_{10}, R_{11})$              | 0.08                                                                        | 0.22                                                              | –                                                   | –                                                                                                |
| $R_{12} = 0.38$                                                   | $(R_{11}, R_{12})$              | 0.12                                                                        | 0.32                                                              | –                                                   | –                                                                                                |
| $R_{13} = 0.54$                                                   | $(R_{12}, R_{13})$              | 0.16                                                                        | 0.46                                                              | Mercury                                             | 0.4                                                                                              |
|                                                                   | $(R_{13}, R_{14})$              | 0.26                                                                        | 0.67                                                              | Venus                                               | 0.7                                                                                              |

Table 1. Continued...

| $R_p$ , the radius of the contracting Solar nebula in units of AU | Annular ring ( $R_{p-1}, R_p$ ) | Width $R_p - R_{p-1}$ of the annular ring ( $R_{p-1}, R_p$ ) in units of AU | Mean radius of the annular ring ( $R_{p-1}, R_p$ ) in units of AU | Known Object in the annular ring ( $R_{p-1}, R_p$ ) | Observed mean distance of the known object in the annular ring ( $R_{p-1}, R_p$ ) in units of AU |
|-------------------------------------------------------------------|---------------------------------|-----------------------------------------------------------------------------|-------------------------------------------------------------------|-----------------------------------------------------|--------------------------------------------------------------------------------------------------|
| $R_{14} = 0.8$                                                    | $(R_{14}, R_{15})$              | 0.33                                                                        | 0.965                                                             | Earth                                               | 1                                                                                                |
| $R_{15} = 1.13$                                                   | $(R_{15}, R_{16})$              | 0.47                                                                        | 1.365                                                             | Mars                                                | 1.5                                                                                              |
| $R_{16} = 1.6$                                                    | $(R_{16}, R_{17})$              | 0.75                                                                        | 1.975                                                             | Asteroids                                           | –                                                                                                |
| $R_{17} = 2.35$                                                   | $(R_{17}, R_{18})$              | 1.05                                                                        | 2.875                                                             | Asteroids                                           | 2.8                                                                                              |
| $R_{18} = 3.4$                                                    | $(R_{18}, R_{19})$              | 1.5                                                                         | 4.15                                                              | Asteroids                                           | –                                                                                                |
| $R_{19} = 4.9$                                                    | $(R_{19}, R_{20})$              | 2.1                                                                         | 5.95                                                              | Jupiter                                             | 5.2                                                                                              |
| $R_{20} = 7$                                                      | $(R_{20}, R_{21})$              | 3.15                                                                        | 8.575                                                             | Saturn                                              | 9.5                                                                                              |
| $R_{21} = 10.15$                                                  | $(R_{21}, R_{22})$              | 4.5                                                                         | 12.4                                                              | Chiron                                              | 13.7                                                                                             |
| $R_{22} = 14.65$                                                  | $(R_{22}, R_{23})$              | 6.47                                                                        | 17.88                                                             | Uranus                                              | 19.2                                                                                             |
| $R_{23} = 21.12$                                                  | $(R_{23}, R_{24})$              | 9.34                                                                        | 25.79                                                             | Neptune                                             | 30.1                                                                                             |
| $R_{24} = 30.46$                                                  | $(R_{24}, R_{25})$              | 13.44                                                                       | 37.18                                                             | Pluto                                               | 39.4                                                                                             |
| $R_{25} = 43.9$                                                   |                                 |                                                                             |                                                                   |                                                     |                                                                                                  |

On the basis of supersonic turbulent convection and the radial turbulent stress and the law of conservation of mass and angular momentum, [13] in the modern Laplacian theory of the Solar System, gets the ratio of the orbital radii  $R_p$  of successively disposed gaseous rings to be a constant given by:

$$R_p/R_{p-1} = \left[1 + \frac{m}{M_f}\right]^2 = \text{Constant} \quad (2.6)$$

Where  $m$  is the mass of the disposed ring,  $M$ , the remaining mass of the protosolar nebula and  $f$ , the moment –of-inertial coefficient. [13] distributed the solar material  $0.05 M_\odot$ , ( $M_\odot = \text{Solar mass}$ ) which has gone to form the planetary system [11,19,20,21,22] among twenty orbits that he got between the present Sun and Neptune, ten between Mercury and the present size of the Sun, and ten between Mercury and Neptune by putting  $m = 1000 M_\oplus$  and  $f = 0.01$  in the eqn (2.6) and got Bodes' constant to be 1.69 which is higher compared to Rawal's which is 1.442. As Rawal is getting twenty five rings between the present Sun and Neptune, each ring in his work gets mass  $660 M_\oplus$ , as its share. Hence putting  $m = 660 M_\oplus$  and  $f = 0.01$ , Rawal found

$$R_p/R_{p-1} = \left[1 + \frac{m}{M_f}\right]^2 = \text{Constant} = 1.442 = a \quad (2.7)$$

This is the difference between Rawal's work and that of Prentice. As geometric series progresses (goes ahead), the planetary distances deviate very much from their real values in Prentice's work, whereas in Rawal's work, the planetary distances remain closer to real values.

Without going into complex details of the theory of supersonic turbulent convection and turbulent stress, when the outward centrifugal force balances the inward gravitational force, that is, considering the rotational evolution of the protosun towards the point of rotational instability, one arrives at the relation Rawal (1986).

$$R_p(\theta)/R_{p-1}(\theta) = \left[1 + \frac{\theta}{2}\right] \quad (2.8)$$

Where  $\theta$  = Inward gravitational force / outward centripetal force.

Thus, one inclines to conclude that during the time, the rotation parameter  $\theta$  increases from 0 and attains the value 1, corresponding to the instability limit, the protosolar nebula decreases its radius from  $R_p$  to  $R_{p-1}$ , where  $R_p$  is the Roche Limit of the Solar nebula, then having radius  $R_{p-1}$ . At this time, supersonic turbulent convection dies down resulting in the steep density inversion at the equator and shading out a ring of matter of width  $(R_p - R_{p-1})$ . At the rotational instability  $\theta \rightarrow 1$  and

$$R_p/R_{p-1} \rightarrow 3/2 = 1.5 \quad (2.9)$$

Just before instability arises

$\theta = 0.9$  and, we have

$$R_p/R_{p-1} = \left(1 + \frac{0.9}{2}\right) = 1.45 = 1.45 \quad (2.10)$$

If  $\theta = 0.89$

$$R_p/R_{p-1} = \left(1 + \frac{0.89}{2}\right) = 1.44 = 1.44 \quad (2.11)$$

This shows superiority of Rawal's work in this case

Several authors [13,15,17,18,1] have arrived at different forms of Titius-Bode Relation in their attempts to explain planetary distances. All were empirical relations. In comparison with those relations, eqn. (2.5) giving outer and inner boundaries of various rings of gas and dust has a physical interpretation, in the sense that it is based on the concept of Roche Limit applied to contracting solar nebula, the halts at various radii are being brought out by the phenomenon of supersonic turbulent convection and the radial turbulent stress, when the outward centrifugal force balances the inward gravitational force, that is, at rotational instability limit, consistent with stable 2/3-Laplacian resonance relation, leading to the formation and detachment of discrete system of rings of gas and dust. This provides an understanding and relation among supersonic turbulent convection and the radial turbulent stress, Roche Limit, rotational instability, stable Laplacian-2/3 resonance, in that rotational instability at the equator of spinning Proto Solar nebula arises at various stages of its quasi-static contraction precisely by the step of Roche Limit (Roche's Constant) consistent with supersonic turbulent convection and the radial turbulent stress and stable Laplacian-2/3 resonance, leading to the formation and detachment of a discrete system of rings of gas and dust, the whole process being controlled by the phenomenon of supersonic turbulent convection and the radial turbulent stress.

The usefulness and novel point of this work is that once the radius of the primary is known, the relation can be set up very simply and uniquely. Interestingly enough, it generates Planetary Distance Law, trying to understand physics behind it and trying to understand physical meaning of constants involved, physics behind the formation of the Solar System. Important

point about this is that if you know the diameter of the central celestial body (a star, galaxy, planet etc.), you know the structure of the whole system. In this connection one should go through [23,24,25].

### 3. CLOSER LOOK AT THE CONTRACTING SOLAR NEBULA

While theorizing and understanding the contraction of the Solar nebula, through the steps of Roche Limit, to understand the formation of the Solar System [4] assumed the ratio  $(\rho_p/\rho_s)$  involved in Roche Limit to be of order unity. Rawal felt that to be closer to reality, one should take closer look at the contracting solar nebula by taking this ratio to be 0.7, 0.8, 0.9, 1.1, 1.2, 1.3 and retrace out the Table 1. Calculations show that the assumption  $(\rho_p/\rho_s) = 1$  may be relaxed, if it is less than 1, the system is narrowed down, and if it is more than 1, the system expands, only the scale-parameter changes, the structure remains similar. However, in all these cases  $(\rho_p/\rho_s) \neq 1$  resonance necessarily will not be stable 2/3-Laplacian resonance. For stable 2/3-Laplacian resonant orbits, the ratios  $(\rho_p/\rho_s) = 1$ , is utmost necessary. One, therefore, concludes that the orbits in the solar system are stable because the ratio  $(\rho_p/\rho_s)$  involved in Roche Limit is of the order unity.

### 4. CONCLUSION

The closer look at the contracting Solar nebula shows that it is not necessary to take the ratio  $(\rho_p/\rho_s)$  involved in the formula for Roche Limit to be unity. This condition may be relaxed. If it is less than 1, the system is narrowed down, and if it is more than 1, the system expands, only the scale parameter changes, the structure remains similar. However, in all these cases  $(\rho_p/\rho_s) \neq 1$  resonance necessarily will not be stable 2/3-Laplacian resonance. For stable 2/3-Laplacian resonant orbits, the ratios  $(\rho_p/\rho_s) = 1$ , is utmost necessary. One, therefore, concludes that the orbits in the solar system are stable because the ratio  $(\rho_p/\rho_s)$  involved in Roche Limit is of the order unity.

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## COMPETING INTERESTS

Authors have declared that no competing interests exist.

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